

# 國立中山大學應用數學系

## 學術演講

講者：朱緒鼎 教授(浙江大學)

講題：Hedetniemi's conjecture and the Poljak-Rödl function (1), (2)

時間：2020/1/20 (Monday) 14:10 ~ 16:00

地點：理學院四樓理 SC 4009-0 多功能互動教室

茶會：13:30 於理 SC 4010 室 (系辦公室)

### Abstract

Hedetniemi conjectured in 1966 that for any graphs  $G, H$ ,  $\chi(G \times H) = \min\{\chi(G), \chi(H)\}$ . This conjecture received a lot of attention in the past half century. It is disproved recently by Shitov. The Poljak-Rödl function is defined as  $f(n) = \min\{\chi(G \times H) : \chi(G) = \chi(H) = n\}$ . Hedetniemi's conjecture is equivalent to say that  $f(n) = n$  for all integer  $n$ . Shitov's result shows that for sufficiently large  $n$ ,  $f(n) < n$ . Using Shitov's result as a blackbox, Tardif and Zhu showed that for sufficiently large  $n$ ,  $f(n) \leq n - (\log n)^{1/4}$ . Using Shitov's method, He and Wigderson showed that for  $\epsilon \approx 10^{-9}$ , for sufficiently large  $n$ ,  $f(n) \leq (1 - \epsilon)n$ . Very recently, I observed that a slight modification of

the proof in the paper by Tardif and Zhu shows that for sufficiently large  $n$ ,  $f(n) \leq \left(\frac{1}{2} + o(1)\right)n$ . On the other hand, it is unknown if  $f(n)$  is bounded by a constant. However, we do know that if  $f(n)$  is bounded by a constant, then the smallest such constant is at most 9. In this lecture, I give self-contained proofs of the above mentioned results.

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