NATIONAL SUN	YAT-SEN UNIVERSITY
IATH 104 / GEAI 12	209: Linear Algebra II
March 21, 2022	Midterm 1
Lecturer: Jeph	ian Lin 林晉宏
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	IATH 104 / GEAI 12 March 21, 2022

5 pages of questions, score page at the end
To be answered: on the test paper Duration: 110 minutes
Total points: 20 points + 2 extra points

Do not open this packet until instructed to do so.

Instructions:

- Enter your Name and Student ID # before you start.
- Using the calculator is not allowed (and not necessary) for this exam.
- Any work necessary to arrive at an answer must be shown on the examination paper. Marks will not be given for final answers that are not supported by appropriate work.
- Clearly indicate your final answer to each question either by underlining it or circling it. If multiple answers are shown then no marks will be awarded.
- 可用中文或英文作答

1. [1pt] What is the elementary matrix corresponding the row operation $\rho_1 \leftrightarrow \rho_2$ applied on matrices with 3 rows? What is its determinant?

2. [1pt] What is the elementary matrix corresponding the row operation ρ_2 : ×2 applied on matrices with 3 rows? What is its determinant?

3. [1pt] What is the elementary matrix corresponding the row operation $\rho_1: +5\rho_2$ applied on matrices with 3 rows? What is its determinant?

4. [2pt] Find a 4×4 matrix A such that det(A) = 5 and every entry of A is nonzero. (Explain why your answer is correct.)

5. Let

$$A = \begin{bmatrix} 1 & 1 & 1 & 1 & 1 \\ 1 & 2 & 4 & 8 & 16 \\ 1 & 3 & 9 & 27 & 81 \\ 1 & 4 & 16 & 64 & 256 \\ 1 & 6 & 36 & 216 & 1296 \end{bmatrix} \text{ and } B = \begin{bmatrix} 1 & 0 & 0 & 0 & x \\ 1 & 2 & 4 & 8 & 16 \\ 1 & 3 & 9 & 27 & 81 \\ 1 & 4 & 16 & 64 & 256 \\ 1 & 6 & 36 & 216 & 1296 \end{bmatrix}$$

(a) [1pt] Find det(A).

(b) [2pt] Find the last row of A^{-1} .

(c) [2pt] Find the x such that det(B) = 0.

6. Show that $det(A) = det(A^{\top})$ for any square matrix A.

7. [5pt] 數學作文:請寫一篇短文來向沒修過線性代數的朋友介紹什麼是 行列式值(determinant)。 請敘述行列式值的定義,並解釋定義中每一條規則的直觀意義。請以 自己的方式、盡量白話的敘述、或是比喻來說明爲什麼要考慮這樣的 概念?請給一些能幫助他人理解的例子,並提出一些這個概念的相關 性質;有必要的話可以加上一些圖來輔助說明。格式沒有限制,篇輻 大約半面到一面。

(If Chinese is not your native language, you may use English or the language that you prefer.)

8. [extra 2pt] Let A be the 9×9 matrix

0	1	0	0	0 0 1 0 1 0 0 0	0	0	0	1	
1	0	1	0	0	0	0	0	0	
0	1	0	1	0	0	0	0	0	
0	0	1	0	1	0	0	0	0	
0	0	0	1	0	1	0	0	0	
0	0	0	0	1	0	1	0	0	
0	0	0	0	0	1	0	1	0	
0	0	0	0	0	0	1	0	1	
1	0	0	0	0	0	0	1	0	
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Find det(A).



Page	Points	Score
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2	5	
3	5	
4	5	
5	2	
Total	20 (+2)	