## 2022F Math589 Midterm 2

5 questions, $20(+5)$ total points
Note: Use other papers to answer the problems. Remember to write down your name and your student ID \#.

1. [5pt] For each of the following properties, find a graph $G$ satisfying the property:
(a) G is not planar.
(b) G is planar but not outerplanar.
(c) G is outerplanar.

Then provide your reasons.
2. [5pt] Let $G$ be the graph below. Find all non-separating induced cycles and one separating induced cycle.

3. [5pt] Show that every bipartite planar graph with $n$ vertices and $m$ edges must have $m \leqslant 2 n-4$. (Note: A bipartite graph is a graph without any odd cycles.)

Two more problems on the back.
4. [5pt] Let $\mathrm{K}_{1,4}$ be the graph below. Find a graph G in $\mathrm{TK}_{1,4}$ with 9 vertices and show it is also a graph in $\mathrm{IK}_{1,4}$.

5. [extra 5 pt ] Let $G$ be the graph below. Find a vertex ordering (e.g., 4, 3, 2, 1, 8, 7, 6, 5) such that the output of the greedy coloring algorithm based on this vertex ordering uses 4 colors.


