姓名 Name：
Quiz 2

學號 Student ID \＃： $\qquad$ MATH 207：Discrete Mathematics II

Let $G$ be the complete graph on vertices $\{0, \ldots, 5\}$ such that the weights of its edges are recorded in the following table．

|  | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 |  | 5 | 19 | 3 | 9 | 4 |
| 1 |  | 16 | 15 | 16 | 13 |  |
| 2 |  |  | 7 | 4 | 16 |  |
| 3 |  |  |  | 1 | 13 |  |
| 4 |  |  |  |  | 14 |  |
| 5 |  |  |  |  |  |  |

Recall that the weight of a spanning tree is the sum of its edge weights．Find a spanning tree of $G$ with the minimum weight．

Check code $=($ weight of your spanning tree $) \bmod 10$

## Solution．

Apply one of the minimum spanning tree algorithms，e．g．，Kruskal＇s algo－ rithm or Prim＇s algorithm．The tree using the following edges

$$
01,24,03,34,05
$$

is a minimum spanning tree，whose weight is 17 ．
Check code $=($ weight of your spanning tree $) \bmod 10=7$ ．

姓名 Name：
Quiz 2

學號 Student ID \＃： $\qquad$ MATH 207：Discrete Mathematics II

Let $G$ be the complete graph on vertices $\{0, \ldots, 5\}$ such that the weights of its edges are recorded in the following table．

|  | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 |  | 2 | 3 | 3 | 12 | 6 |
| 1 |  | 10 | 9 | 20 | 7 |  |
| 2 |  |  | 20 | 2 | 19 |  |
| 3 |  |  |  | 6 | 14 |  |
| 4 |  |  |  |  | 13 |  |
| 5 |  |  |  |  |  |  |

Recall that the weight of a spanning tree is the sum of its edge weights．Find a spanning tree of $G$ with the minimum weight．

Check code $=($ weight of your spanning tree $) \bmod 10$

## Solution．

Apply one of the minimum spanning tree algorithms，e．g．，Kruskal＇s algo－ rithm or Prim＇s algorithm．The tree using the following edges

$$
01,02,03,24,05
$$

is a minimum spanning tree，whose weight is 16 ．
Check code $=($ weight of your spanning tree $) \bmod 10=6$ ．

Indicating your answer by underlining it or circling it． Compute the check code and fill it into the box on the right．

姓名 Name：
Quiz 2

學號 Student ID \＃： $\qquad$ MATH 207：Discrete Mathematics II

Let $G$ be the complete graph on vertices $\{0, \ldots, 5\}$ such that the weights of its edges are recorded in the following table．

|  | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 |  | 8 | 19 | 18 | 5 | 12 |
| 1 |  | 20 | 16 | 19 | 3 |  |
| 2 |  |  | 20 | 1 | 16 |  |
| 3 |  |  |  | 9 | 18 |  |
| 4 |  |  |  |  | 8 |  |
| 5 |  |  |  |  |  |  |

Recall that the weight of a spanning tree is the sum of its edge weights．Find a spanning tree of $G$ with the minimum weight．

Check code $=($ weight of your spanning tree $) \bmod 10$

## Solution．

Apply one of the minimum spanning tree algorithms，e．g．，Kruskal＇s algo－ rithm or Prim＇s algorithm．The tree using the following edges

$$
15,24,34,04,45
$$

is a minimum spanning tree，whose weight is 26 ．
Check code $=($ weight of your spanning tree $) \bmod 10=6$ ．
 Compute the check code and fill it into the box on the right．

姓名 Name：
Quiz 2

學號 Student ID \＃： $\qquad$ MATH 207：Discrete Mathematics II

Let $G$ be the complete graph on vertices $\{0, \ldots, 5\}$ such that the weights of its edges are recorded in the following table．

|  | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 |  | 8 | 10 | 4 | 13 | 16 |
| 1 |  | 5 | 3 | 3 | 1 |  |
| 2 |  |  | 13 | 18 | 10 |  |
| 3 |  |  |  | 2 | 8 |  |
| 4 |  |  |  |  | 17 |  |
| 5 |  |  |  |  |  |  |

Recall that the weight of a spanning tree is the sum of its edge weights．Find a spanning tree of $G$ with the minimum weight．

Check code $=($ weight of your spanning tree $) \bmod 10$

## Solution．

Apply one of the minimum spanning tree algorithms，e．g．，Kruskal＇s algo－ rithm or Prim＇s algorithm．The tree using the following edges

$$
13,12,03,34,15
$$

is a minimum spanning tree，whose weight is 15 ．
Check code $=($ weight of your spanning tree $) \bmod 10=5$ ．

姓名 Name：
Quiz 2

學號 Student ID \＃： $\qquad$ MATH 207：Discrete Mathematics II

Let $G$ be the complete graph on vertices $\{0, \ldots, 5\}$ such that the weights of its edges are recorded in the following table．

|  | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 |  | 20 | 9 | 12 | 17 | 1 |
| 1 |  |  | 15 | 8 | 2 | 6 |
| 2 |  |  |  | 4 | 12 | 16 |
| 3 |  |  |  | 8 | 13 |  |
| 4 |  |  |  |  |  | 18 |
| 5 |  |  |  |  |  |  |

Recall that the weight of a spanning tree is the sum of its edge weights．Find a spanning tree of $G$ with the minimum weight．

Check code $=($ weight of your spanning tree $) \bmod 10$

## Solution．

Apply one of the minimum spanning tree algorithms，e．g．，Kruskal＇s algo－ rithm or Prim＇s algorithm．The tree using the following edges

$$
15,23,13,14,05
$$

is a minimum spanning tree，whose weight is 21 ．
Check code $=($ weight of your spanning tree $) \bmod 10=1$ ．


姓名 Name：
Quiz 2

學號 Student ID \＃： $\qquad$ MATH 207：Discrete Mathematics II

Let $G$ be the complete graph on vertices $\{0, \ldots, 5\}$ such that the weights of its edges are recorded in the following table．

|  | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 |  | 19 | 3 | 16 | 9 | 2 |
| 1 |  | 1 | 5 | 19 | 16 |  |
| 2 |  |  |  | 12 | 11 | 1 |
| 3 |  |  |  | 9 | 16 |  |
| 4 |  |  |  |  | 7 |  |
| 5 |  |  |  |  |  |  |

Recall that the weight of a spanning tree is the sum of its edge weights．Find a spanning tree of $G$ with the minimum weight．

Check code $=($ weight of your spanning tree $) \bmod 10$

## Solution．

Apply one of the minimum spanning tree algorithms，e．g．，Kruskal＇s algo－ rithm or Prim＇s algorithm．The tree using the following edges

$$
12,25,13,45,05
$$

is a minimum spanning tree，whose weight is 16 ．
Check code $=($ weight of your spanning tree $) \bmod 10=6$ ．

姓名 Name：
Quiz 2

學號 Student ID \＃： $\qquad$ MATH 207：Discrete Mathematics II

Let $G$ be the complete graph on vertices $\{0, \ldots, 5\}$ such that the weights of its edges are recorded in the following table．

|  | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 11 | 5 | 13 | 2 | 3 |  |
| 1 |  |  | 18 | 4 | 12 | 19 |
| 2 |  |  |  | 2 | 17 | 7 |
| 3 |  |  |  |  | 2 | 3 |
| 4 |  |  |  |  |  | 14 |
| 5 |  |  |  |  |  |  |

Recall that the weight of a spanning tree is the sum of its edge weights．Find a spanning tree of $G$ with the minimum weight．

Check code $=($ weight of your spanning tree $) \bmod 10$

## Solution．

Apply one of the minimum spanning tree algorithms，e．g．，Kruskal＇s algo－ rithm or Prim＇s algorithm．The tree using the following edges

$$
13,23,34,04,05
$$

is a minimum spanning tree，whose weight is 13 ．
Check code $=($ weight of your spanning tree $) \bmod 10=3$ ．

Indicating your answer by underlining it or circling it． Compute the check code and fill it into the box on the right．

姓名 Name：
Quiz 2

學號 Student ID \＃： $\qquad$ MATH 207：Discrete Mathematics II

Let $G$ be the complete graph on vertices $\{0, \ldots, 5\}$ such that the weights of its edges are recorded in the following table．

|  | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 |  | 8 | 12 | 13 | 5 | 7 |
| 1 |  |  | 2 | 3 | 5 | 8 |
| 2 |  |  |  | 17 | 7 | 13 |
| 3 |  |  |  |  | 1 | 15 |
| 4 |  |  |  |  |  | 16 |
| 5 |  |  |  |  |  |  |

Recall that the weight of a spanning tree is the sum of its edge weights．Find a spanning tree of $G$ with the minimum weight．

Check code $=($ weight of your spanning tree $) \bmod 10$

## Solution．

Apply one of the minimum spanning tree algorithms，e．g．，Kruskal＇s algo－ rithm or Prim＇s algorithm．The tree using the following edges

$$
13,12,34,04,05
$$

is a minimum spanning tree，whose weight is 18 ．
Check code $=($ weight of your spanning tree $) \bmod 10=8$ ．

姓名 Name：
Quiz 2

學號 Student ID \＃： $\qquad$ MATH 207：Discrete Mathematics II

Let $G$ be the complete graph on vertices $\{0, \ldots, 5\}$ such that the weights of its edges are recorded in the following table．

|  | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 |  | 15 | 20 | 12 | 9 | 5 |
| 1 |  |  | 6 | 1 | 11 | 17 |
| 2 |  |  |  | 15 | 20 | 3 |
| 3 |  |  |  |  | 11 | 18 |
| 4 |  |  |  |  |  | 20 |
| 5 |  |  |  |  |  |  |

Recall that the weight of a spanning tree is the sum of its edge weights．Find a spanning tree of $G$ with the minimum weight．

Check code $=($ weight of your spanning tree $) \bmod 10$

## Solution．

Apply one of the minimum spanning tree algorithms，e．g．，Kruskal＇s algo－ rithm or Prim＇s algorithm．The tree using the following edges

$$
12,25,13,04,05
$$

is a minimum spanning tree，whose weight is 24 ．
Check code $=($ weight of your spanning tree $) \bmod 10=4$ ．

姓名 Name：
Quiz 2

學號 Student ID \＃： $\qquad$ MATH 207：Discrete Mathematics II

Let $G$ be the complete graph on vertices $\{0, \ldots, 5\}$ such that the weights of its edges are recorded in the following table．

|  | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 |  | 19 | 2 | 14 | 16 | 19 |
| 1 |  | 1 | 7 | 15 | 16 |  |
| 2 |  |  |  | 9 | 6 | 2 |
| 3 |  |  |  | 17 | 16 |  |
| 4 |  |  |  |  | 11 |  |
| 5 |  |  |  |  |  |  |

Recall that the weight of a spanning tree is the sum of its edge weights．Find a spanning tree of $G$ with the minimum weight．

Check code $=($ weight of your spanning tree $) \bmod 10$

## Solution．

Apply one of the minimum spanning tree algorithms，e．g．，Kruskal＇s algo－ rithm or Prim＇s algorithm．The tree using the following edges

$$
12,02,13,24,25
$$

is a minimum spanning tree，whose weight is 18 ．
Check code $=($ weight of your spanning tree $) \bmod 10=8$ ．

