## Math589 Homework 2

**Note:** To submit the k-th homework, simply put your files in the folder HWk on CoCalc, and it will be collected on the due day.

1. Suppose G is a simple graph on n vertices and m edges. Show that if  $m \le n-2$  then G is not connected.

**Solution.** Start from n isolated vertices. (That is, a graph on n vertices without any edge.) When an edge is added, it at most combines two components into one component. This operation decreases the number of components by at most one. If  $m \leq n-2$  edges were added, then the number of components is at least  $n - m \geq 2$ , so G is not connected.

2. Find two distinct graphs on 4 vertices with 3 edges.

**Solution.** Each of the following two graphs has 4 vertices and 3 edges.

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