國立中山大學跨領域及數據科學研究中心 國立中山大學應用數學系 學術演講

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講 題: Kummer and gamma distributions through Matsumoto-Yor type properties

時 間:2015/11/05(星期四)14:10~15:00

地 點:理學院四樓理 SC 4009-1 室

茶 會:15:00 於理 SC 4010 室 (系辦公室)

摘要

Koudu and Vallois (2012) looked for distributions of independent random variables X and Y and a function f having the property that f(X+Y) and f(X)-f(X+Y) are independent and related characterizations. Their starting point was the Matsumoto-Yor (MY) property, which is obtained by taking X of the GIG distribution, Y of the gamma distribution and f(x)=1/x. Note also that the famous Lukacs property is obtained by taking $f(x)=\log(x)$. An analogue involving Kummer and gamma distributions is when $f(x)=\log(1+1/x)$. However their characterization needed assumption of smoothness of strictly positive densities. We will show how the densities can be avoided by considering even a weaker constancy of regressions conditions. Also a characterization connected to a new MY-related independence property for Kummer and gamma laws discovered recently in Hamza and Vallois (2015) will be presented. The main issue in this context is a multivariate setting defined in terms of directed trees (an analogy to the classical MY case). More can be found in:

- 1. Hamza, M., Vallois, P., On Kummer's distributions od type two and generalized beta distributions, Statis. Probab. Lett. (2015) submitted.
- 2. Koudu, E., Vallois, P., Independence properties of the Matsumoto-Yor type. Bernoulli 18(1) (2012), 119-136.
- 3. Letac, G., Wesołowski, J., On an independence property for the product of GIG and Gamma laws. Annals of Probability 28 (2000), 1371-1383.
- 4. Massam, H., Wesołowski, J., The Matsumoto-Yor property on trees. Bernoulli 10 (2004), 685-700.
- 5. Piliszek, A., Wesołowski, J., Univariate and multivariate characterization of the Kummer and gamma laws, Bernoulli (2015) submitted.
- 6. Wesołowski, J., On the Matsumoto-Yor type regression characterization of the gamma and Kummer distributions. Statistics and Probability Letters 107 (2015), 145-149.

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